

Investigation of double frequency fishbones in EAST with neutral beam injection

Wei Shen¹, Shengfa Wu¹, Liqing Xu¹, Zhiyong Qiu¹, Yan Chao², Yifeng Wang¹, Yuqi Chu¹, Jianwen Liu¹,
Baolong Hao³, Ming Xu¹, Yinfei Jin¹, Guoqiang Zhong¹, and EAST Team

¹ Institute of Plasma Physics, Chinese Academy of Science, China

² Shenzhen University, Shenzhen, China

³ Southwestern Institute of Physics, Chengdu, China

Outline

➤ **Background**

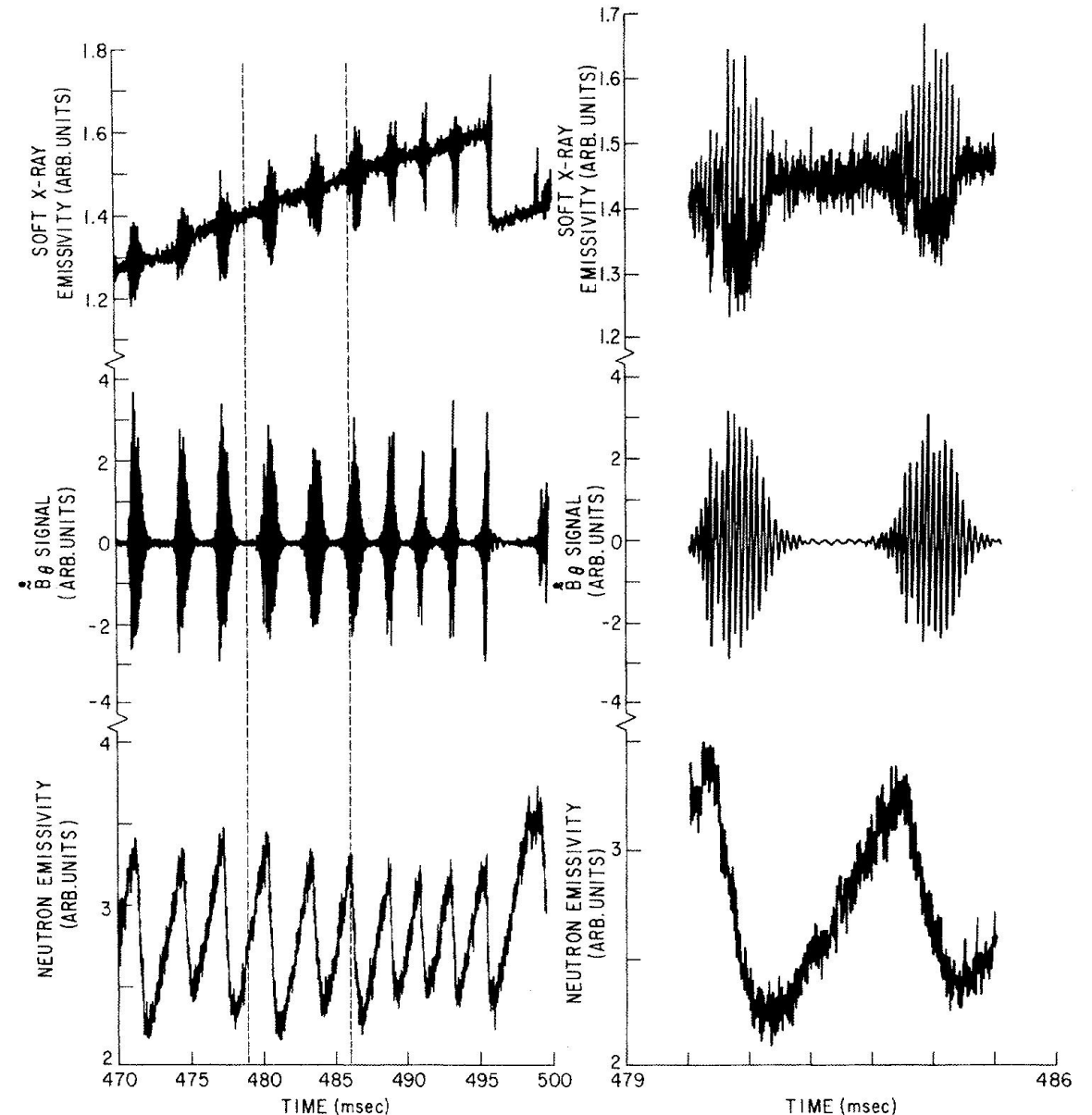
➤ **Experimental observations**

➤ **Simulation results**

➤ **Summary**

Background

- Energetic particle driven instabilities, such as fishbones and various Alfvén eigenmodes, can induce energetic particle loss, degrade fast particle confinement, and even lead to serious damage of the first wall.
- Fishbone was first discovered in PDX with NBI[K. McGuire et al. PRL 1983], which is typically an internal mode with toroidal mode number $n = 1$ and dominant poloidal mode number $m = 1$.



Background: precessional fishbone

- Two theories were developed to explain the fishbone.
- Chen et al.[L. Chen et al. PRL 1983] proposed that the fishbone is driven by energetic trapped ions via precessional resonant condition $\omega = \omega_d$.
- Coppi et al.[B. Coppi et al PRL 1986] proposed that fishbone is destabilized by energetic particles through a positive dissipation process with the mode frequency on the order of ω_{*i} .
- Fishbone dispersion relation based on Chen's theory: [L. Chen et al. PRL 1983](#)

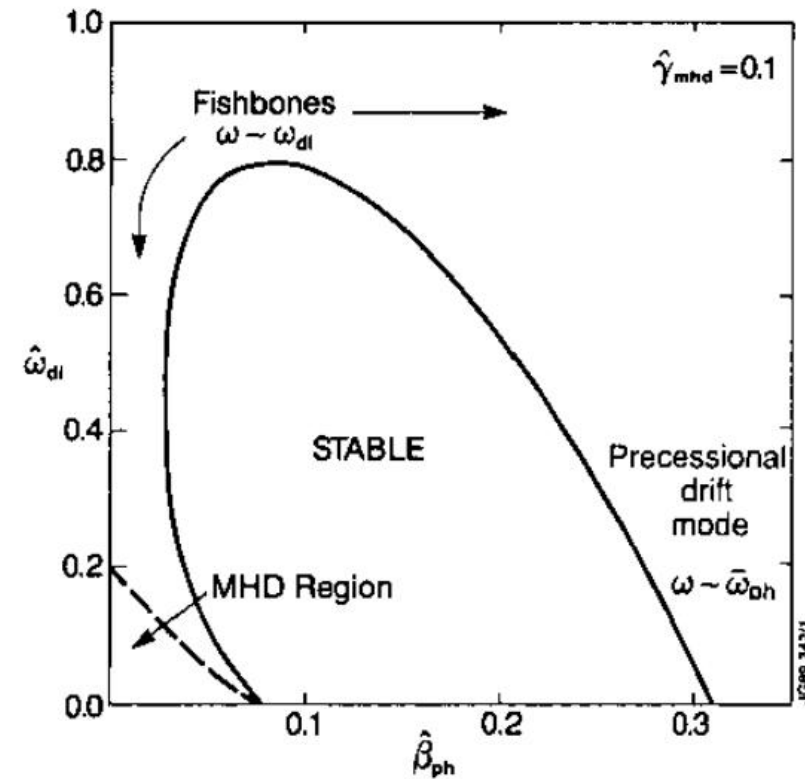
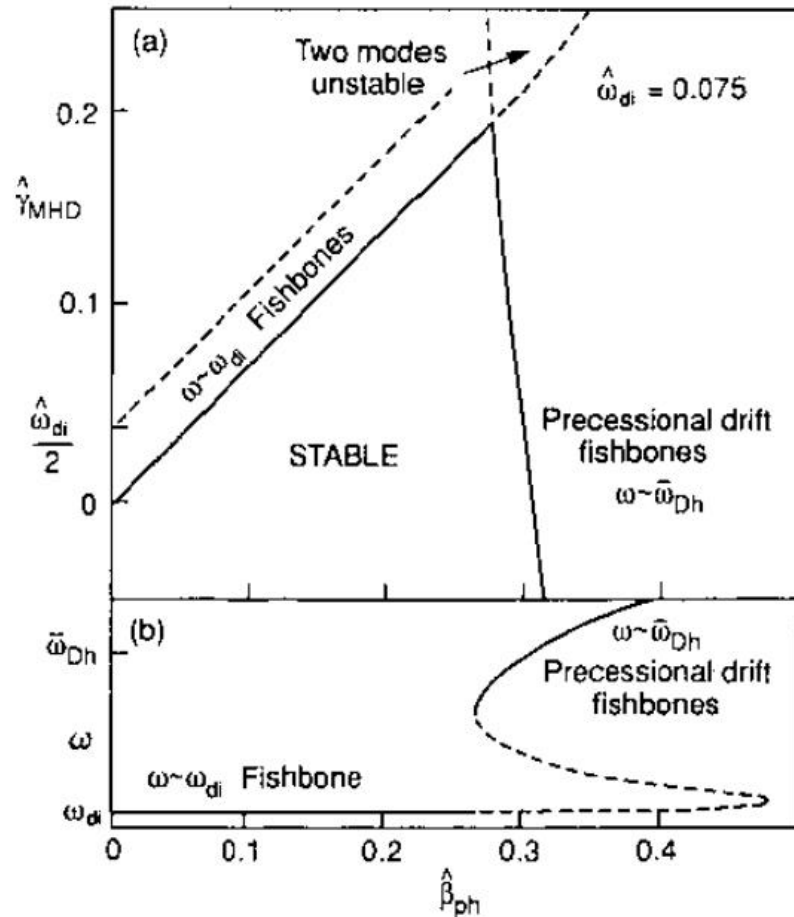
initial term **fluid** **energetic particle**

$$-i\omega/\tilde{\omega}_A + \delta\hat{W}_f + \delta\hat{W}_k = 0$$

$$\delta\hat{W}_k = \frac{\pi^2 m_h 2^{7/2}}{(r_s B_0)^2} \int_0^{r_s} r dr \int_{1-r/R}^{1+r/R} d(\alpha B) \int_0^\infty dE E^{5/2} \frac{K_2^2}{K_b} \left[\frac{Q}{\tilde{\omega}_{dh} - \omega} \right]_{1,1}$$

Background: stability diagram

- Stability diagram of precessional fishbone and diamagnetic fishbone (Porcelli, PPCF 1991)
- When EP beta exceeds a critical value, precessional fishbone is excited



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Experimental setup and observations

- In this work, the global hybrid code M3D-K is applied to analyse the fishbones with mode numbers $m/n=1/1$ and $2/2$ observed in EAST with neutral beam injection.

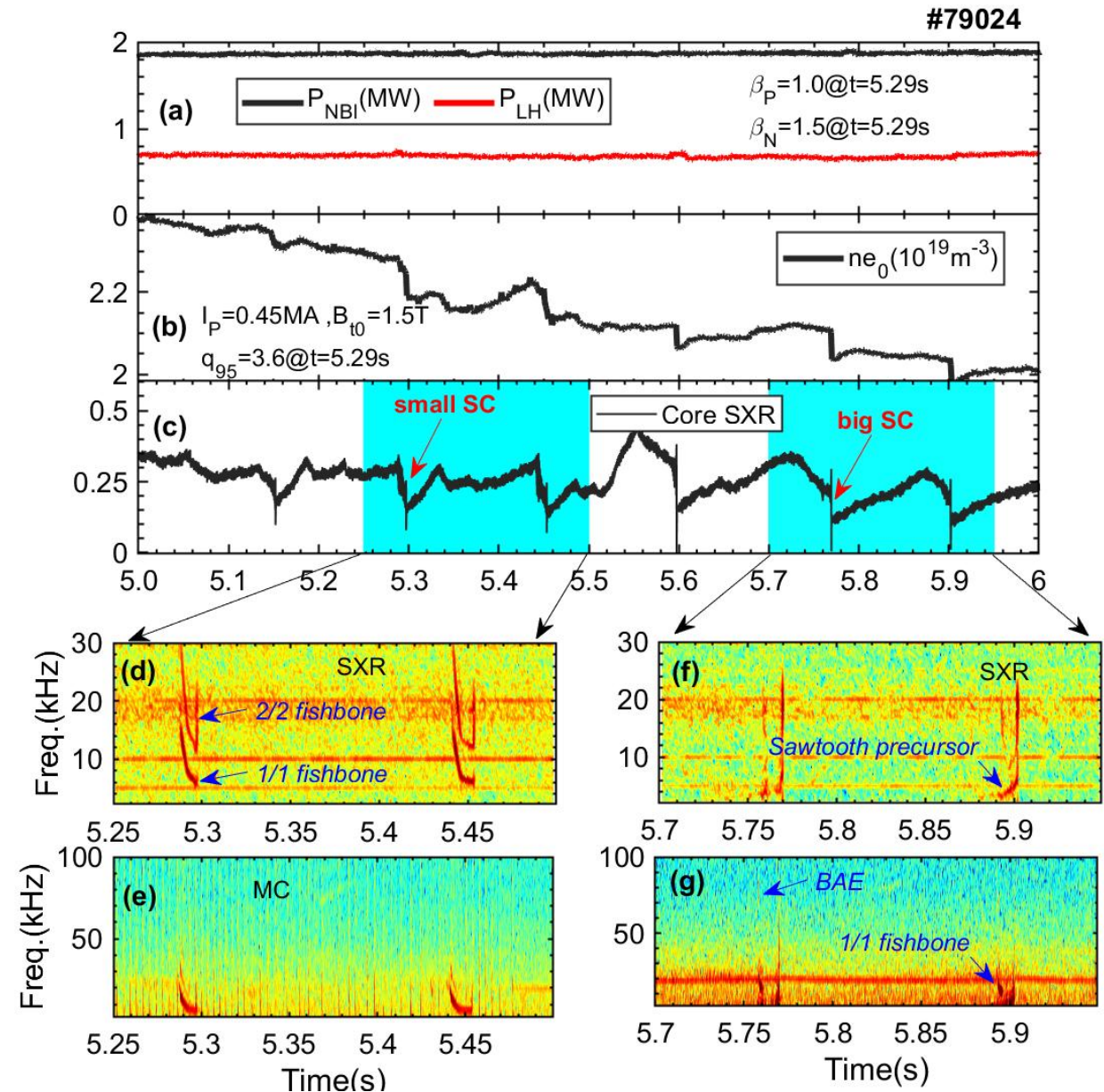
$P_{\text{NBI}} \sim 2$ MW with injected energy 60 keV

$I_p = 0.45$ MA

$P_{\text{LH}} \sim 0.8$ MW

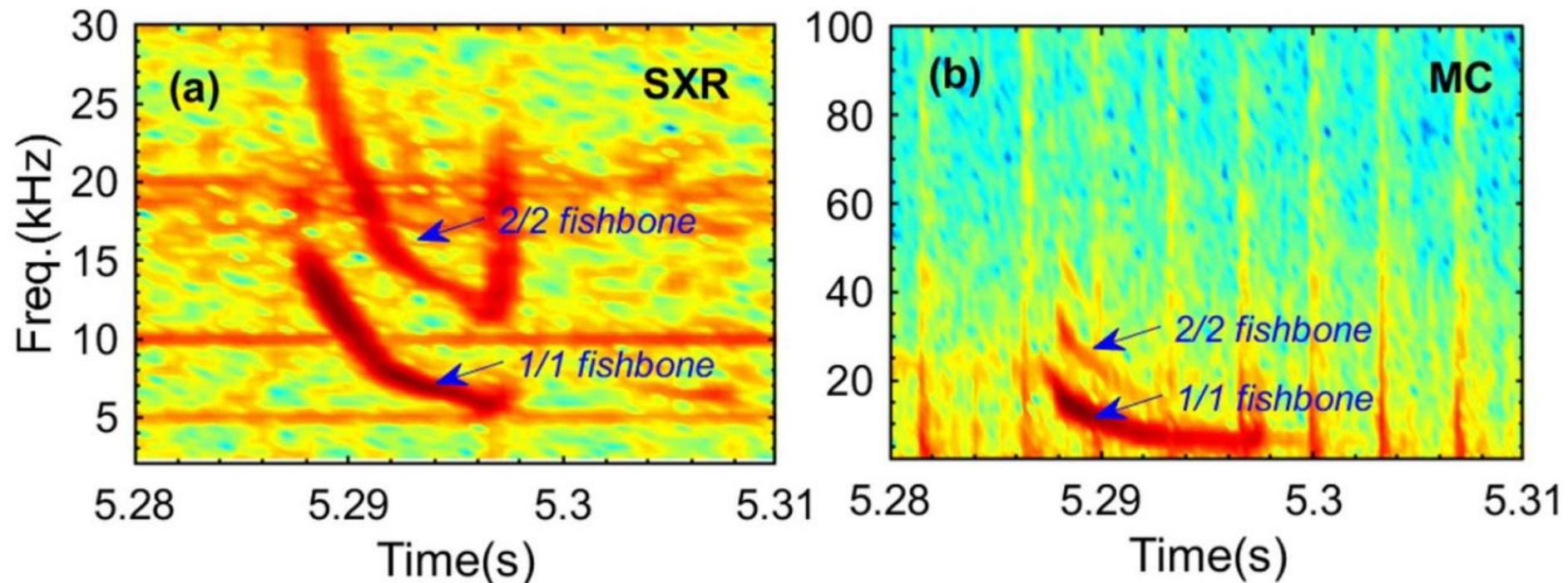
$B_t = 1.5$ T

$q_{95} \sim 3.6$



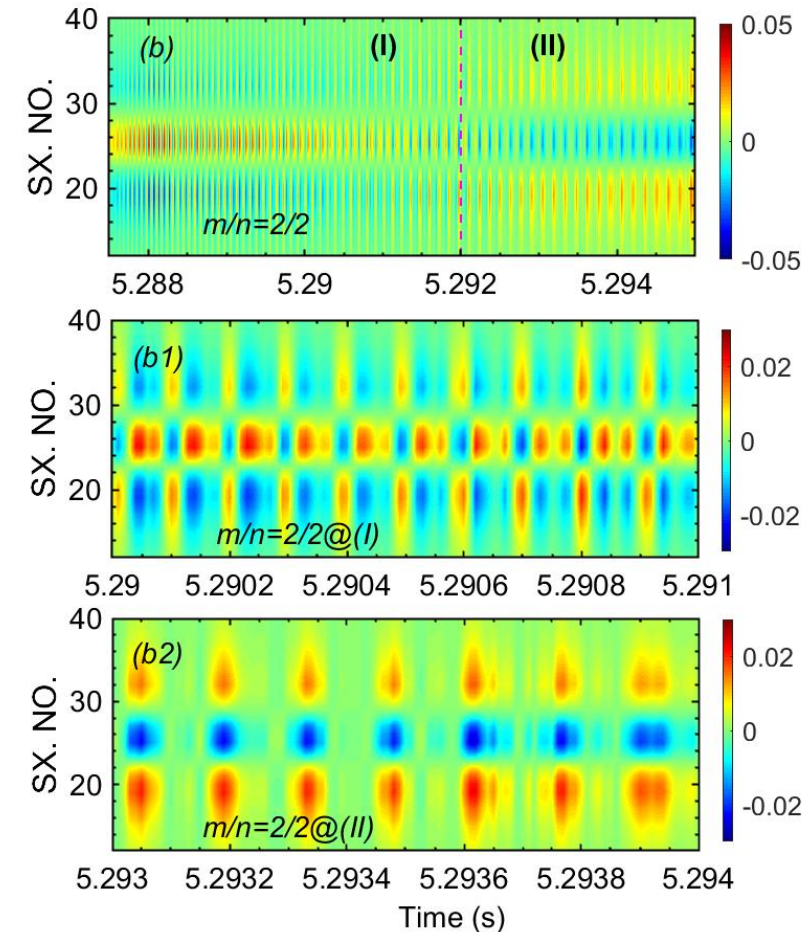
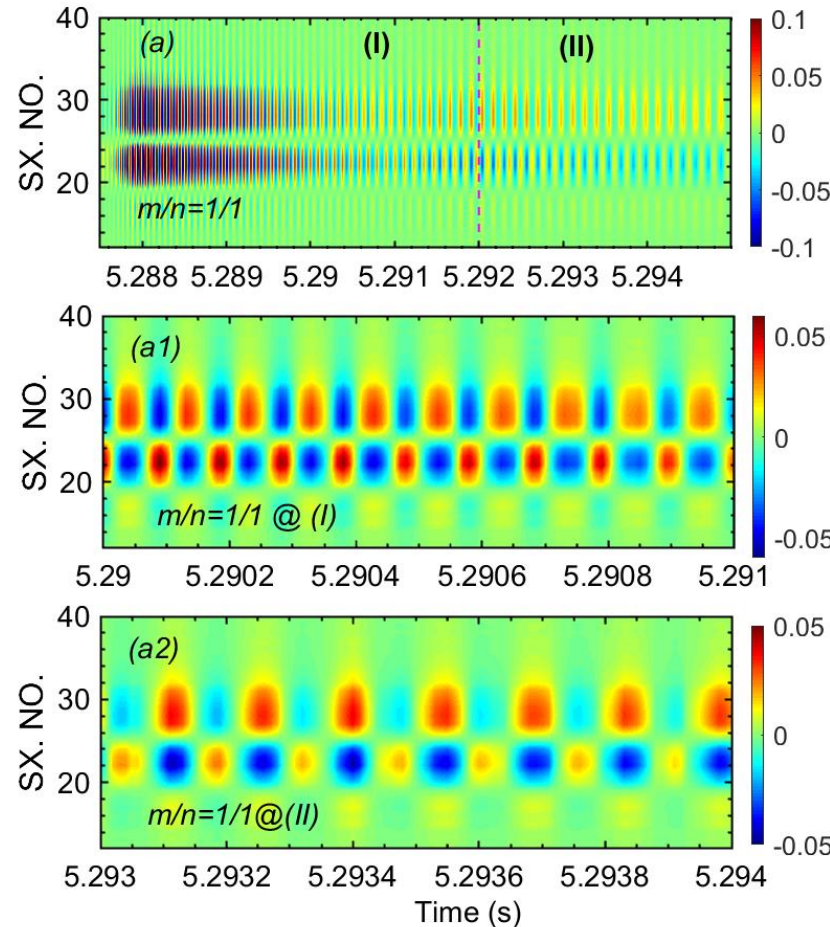
Double frequency fishbones are observed in EAST

- The presence of a fishbone mode with $m/n = 2/2$ that rivals the fundamental $m/n = 1/1$ mode. The frequency of the $m/n = 2/2$ mode is double of the $m/n = 1/1$ fishbone mode.
- The frequency of the fundamental fishbone mode undergoes a decrease from an initial $f \sim 20$ kHz to $f \sim 7$ kHz.



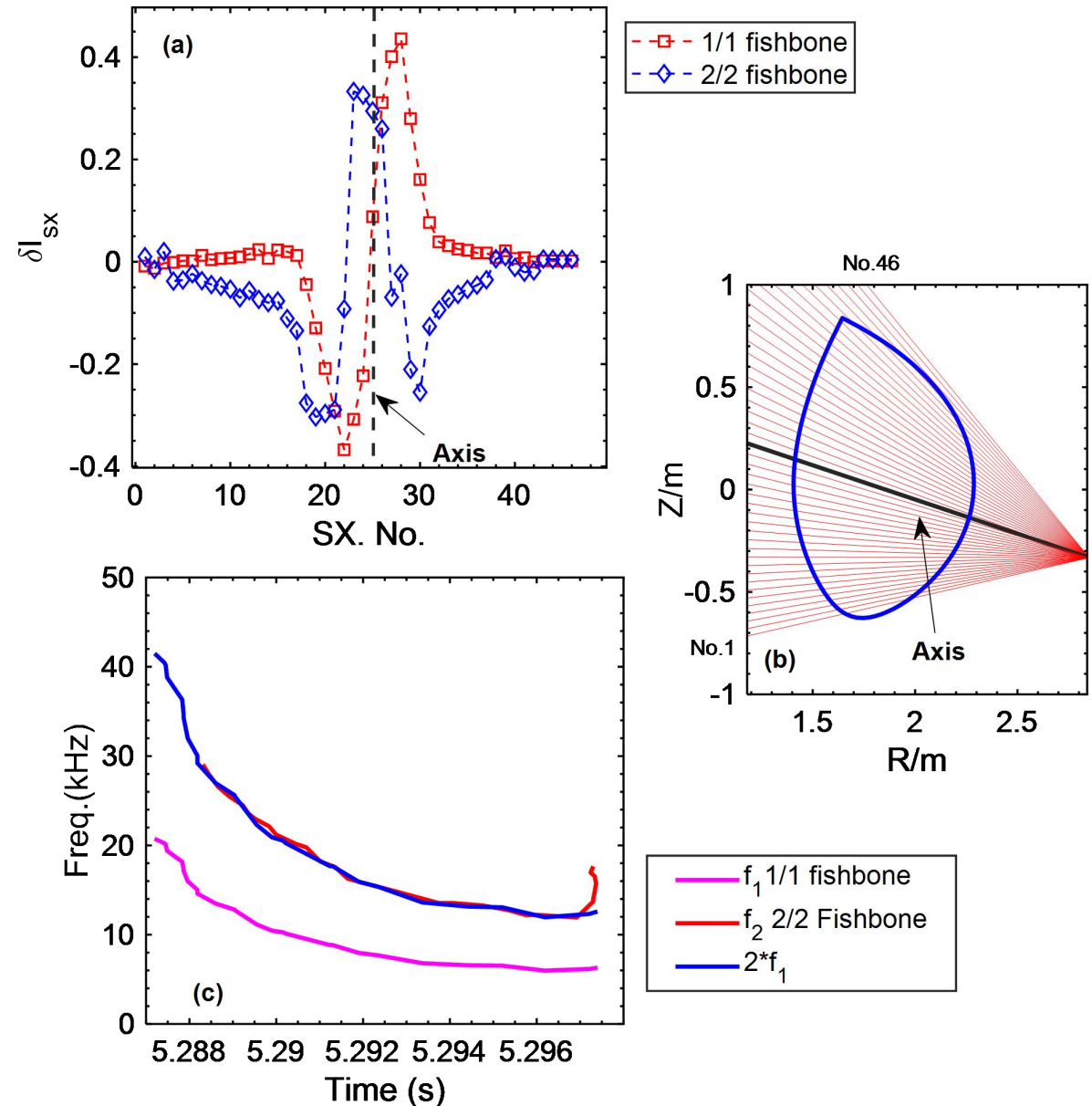
SXR structure of both $m/n=1/1$ and $m/n=2/2$ modes

- Both modes are situated at the same radial location.
- phase I: $m/n=1/1$ amplitude is stronger than that of $m/n=2/2$ mode.
- phase II: $m/n=1/1$ mode saturates, while $m/n=2/2$ fishbone increases



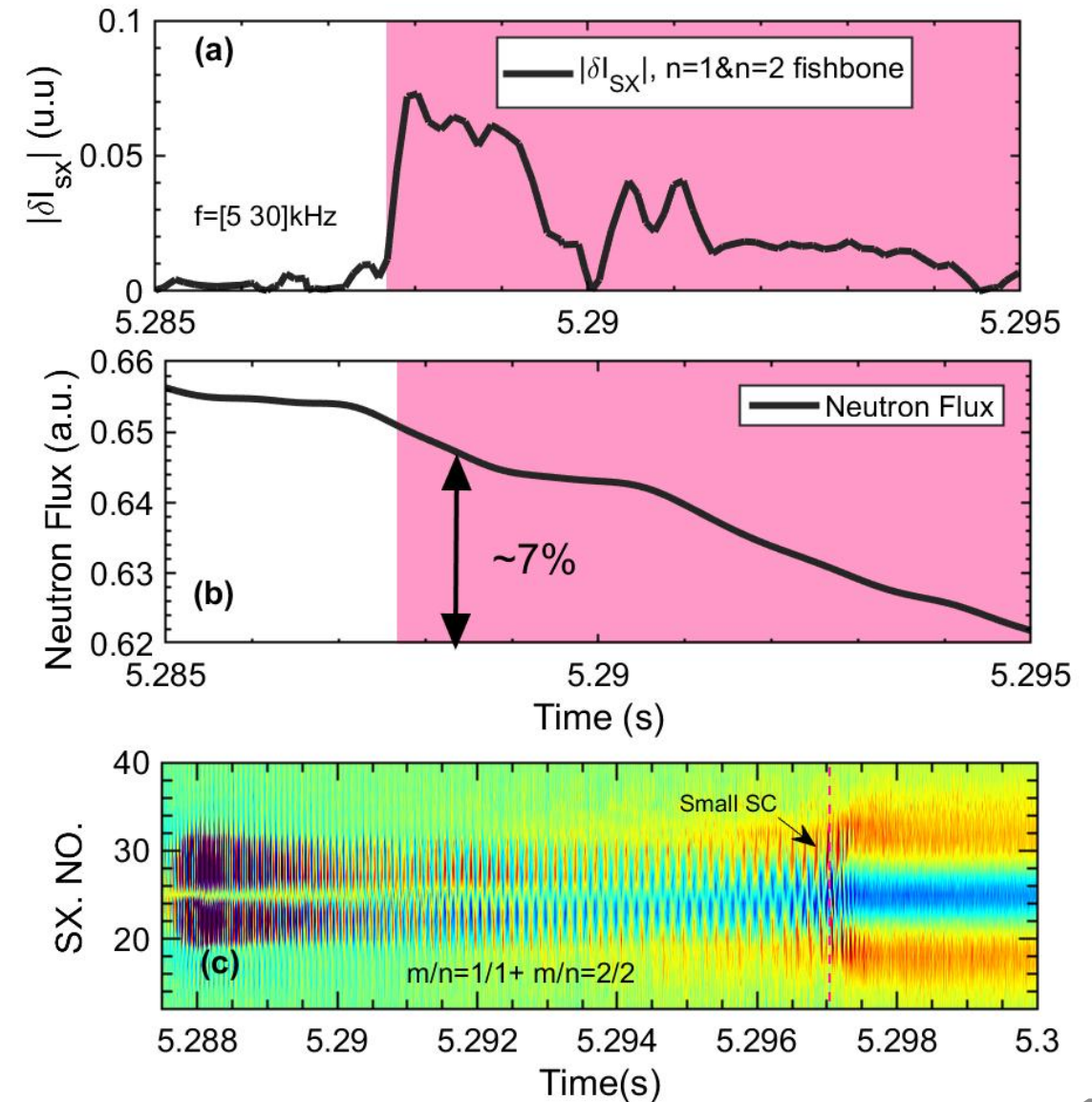
Fishbone mode structure and frequency

- Figure (a) shows the $n = 1$ mode exhibits an odd symmetry structure, whereas the $n = 2$ mode displays an even symmetry structure.
- Figure (c) shows the $n = 2$ fishbone mode occurs following the $n = 1$ fishbone mode. The frequency of the $n = 2$ mode is double that of the $n = 1$ mode



Neutron flux drops during fishbone evolution

- In EAST, neutron flux evolution is used to monitor the dynamics of energetic ions produced by NBI in the core region.
- A drop of neutron flux around 7% is observed during fishbones with $m/n=1/1$ and $m/n=2/2$ components.



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M3D-K model

resistive MHD+EP pressure coupling

$$\rho \frac{d\mathbf{v}}{dt} = -\nabla P - \nabla \cdot \mathbf{P}_h + \mathbf{J} \times \mathbf{B}$$

$$\mathbf{J} = \nabla \times \mathbf{B}, \quad \frac{\partial \mathbf{B}}{\partial t} = -\nabla \times \mathbf{E}$$

$$\mathbf{E} + \mathbf{v} \times \mathbf{B} = \eta \mathbf{J}$$

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\frac{dp}{dt} = -\gamma p \nabla \cdot \mathbf{v} + \rho \nabla \cdot \overleftrightarrow{\kappa} \cdot \nabla \frac{p}{\rho}$$

CGL form

$$\mathbf{P}_h = P_{\perp} \mathbf{I} + (P_{\parallel} - P_{\perp}) \mathbf{b} \mathbf{b}$$

guiding center distribution

$$F = F(\mathbf{X}, v_{\parallel}, \mu) = \sum_i \delta(\mathbf{X} - \mathbf{X}_i) \delta(v_{\parallel} - v_{\parallel,i}) \delta(\mu - \mu_i)$$

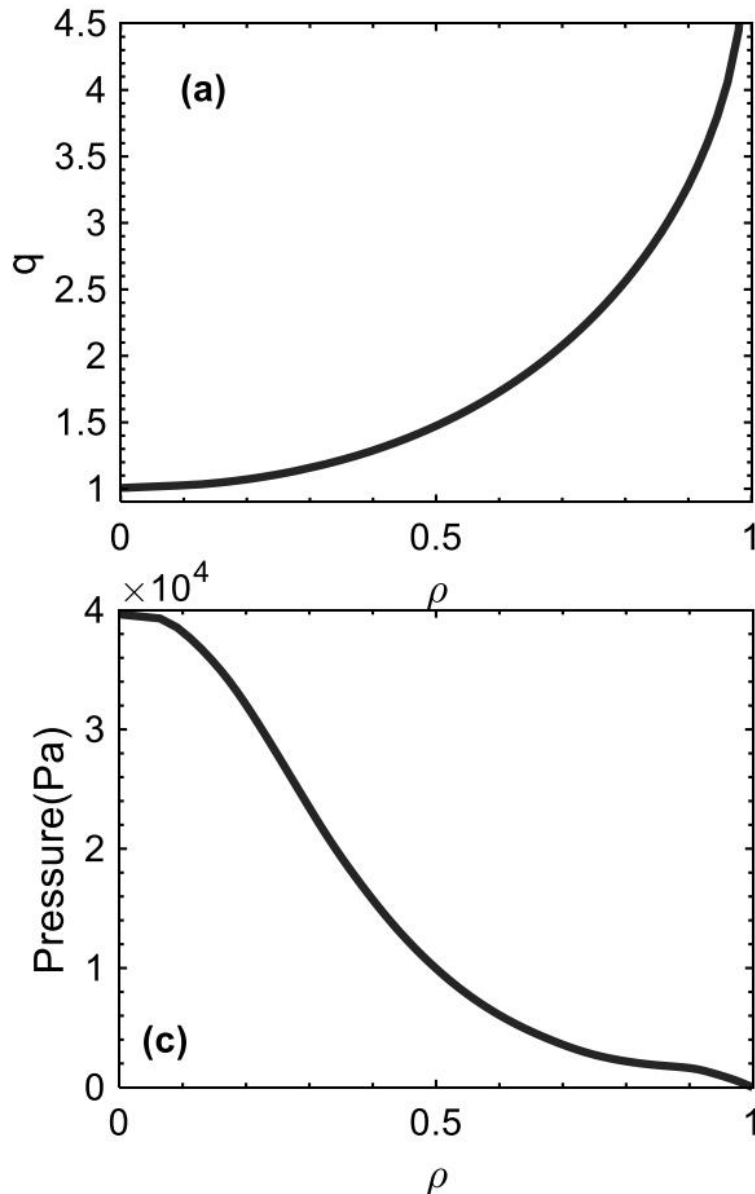
gyro-kinetic/drift kinetic equations

$$\frac{d\mathbf{X}}{dt} = \frac{1}{B^{**}} [v_{\parallel} \mathbf{B}^* - \mathbf{b}_0 \times (\langle \mathbf{E} \rangle - \frac{1}{e} \mu \nabla (B_0 + \langle \delta B \rangle))]]$$

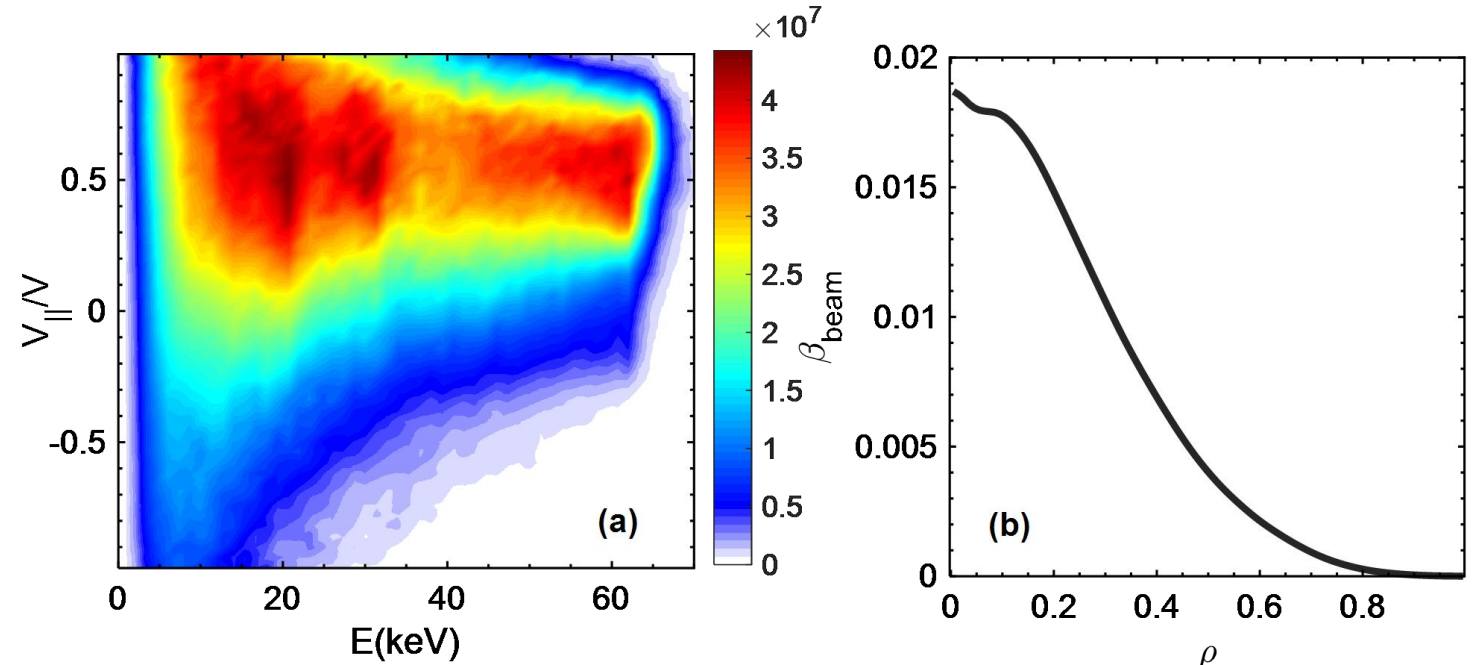
$$m \frac{dv_{\parallel}}{dt} = \frac{e}{B^{**}} \mathbf{B}^* \cdot [\langle \mathbf{E} \rangle - \frac{1}{e} \mu \nabla (B_0 + \langle \delta B \rangle)]$$

$$\mathbf{B}^* = \mathbf{B}_0 + \langle \delta \mathbf{B} \rangle + \frac{mv_{\parallel}}{q} \nabla \times \mathbf{b}_0, \quad B^{**} = \mathbf{B}^* \cdot \mathbf{b}_0$$

Initial profiles and parameters set up

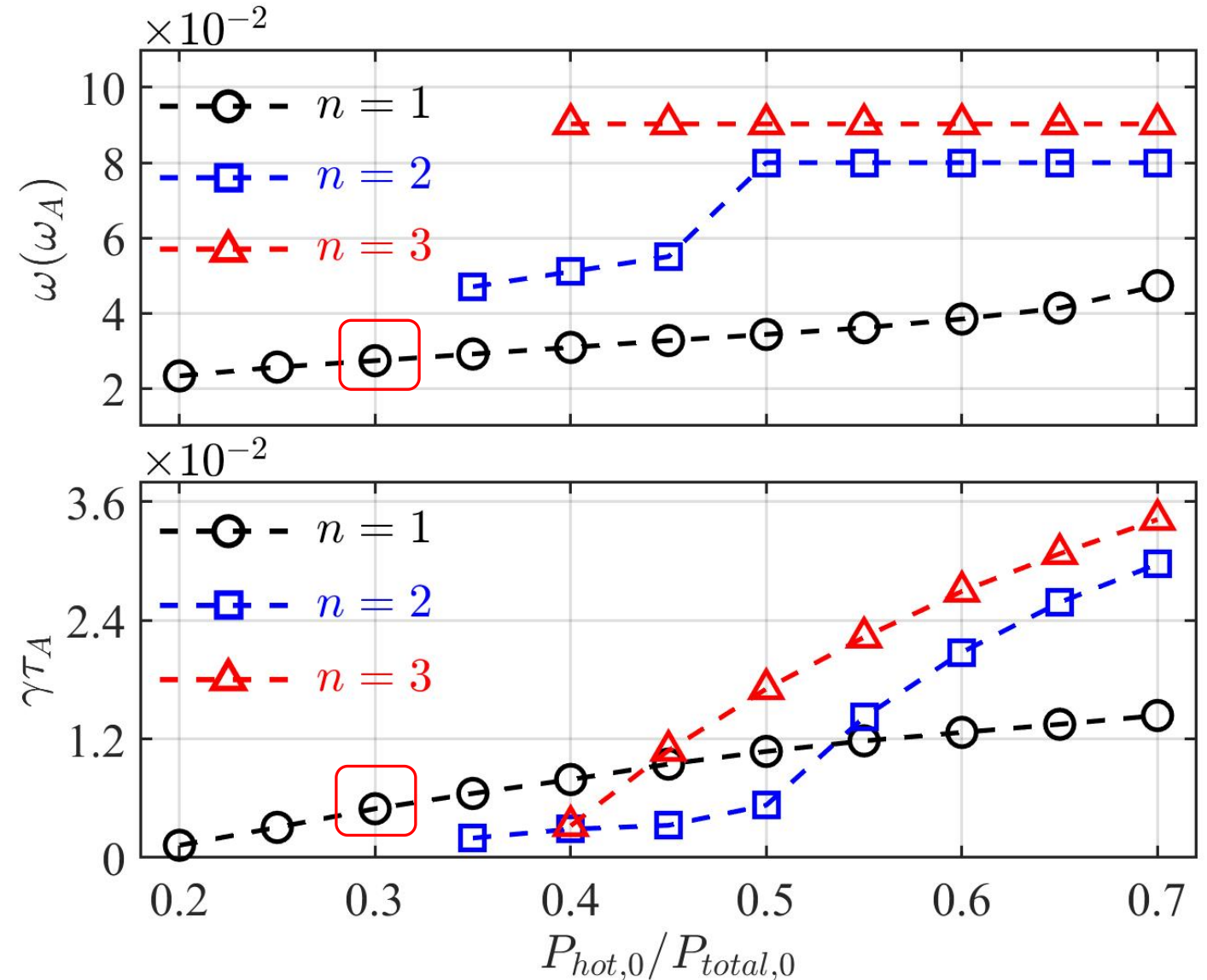


- Initial profiles and parameters are chosen at $t=5.288$ s of #Shot 79024



High order harmonis is excited when EP pressure increases

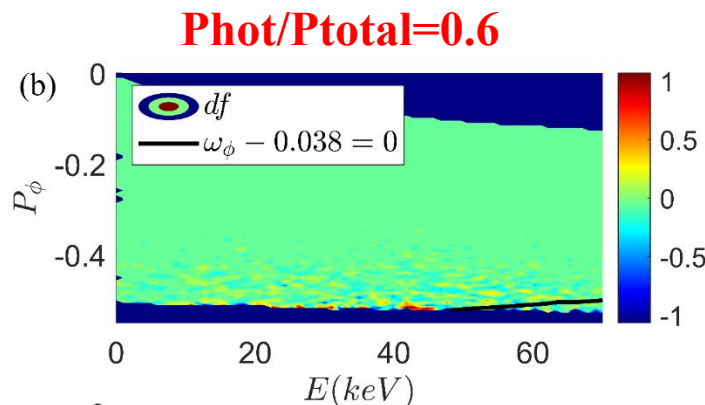
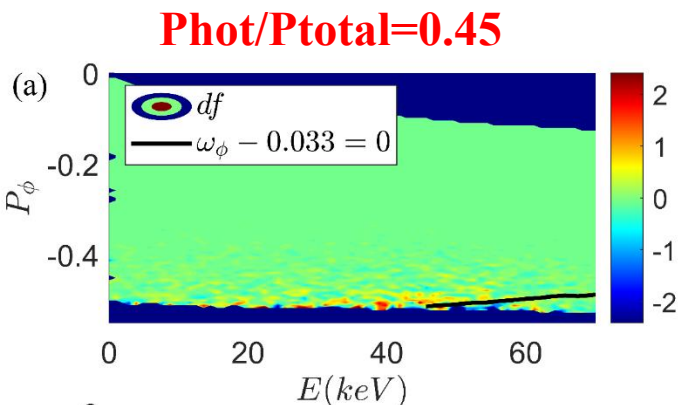
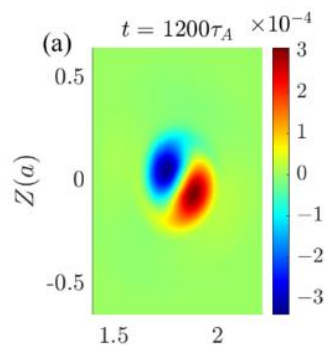
- $m/n=1/1$ fishbone is excited when $P_{hot,0}/P_{total,0} > 0.2$
- when EP pressure increases futher, $n=2$ and $n=3$ modes are driven unstable.



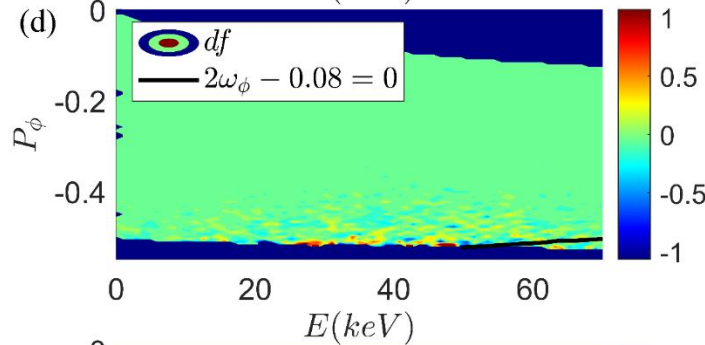
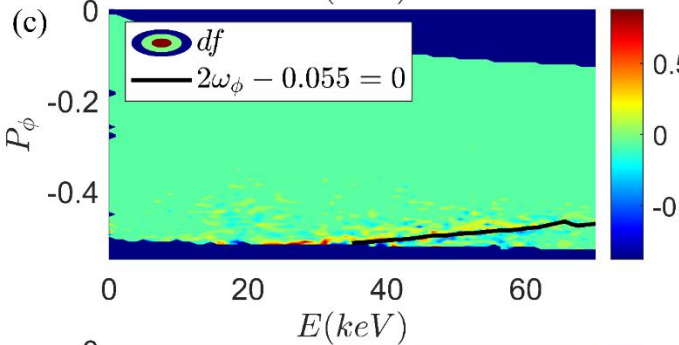
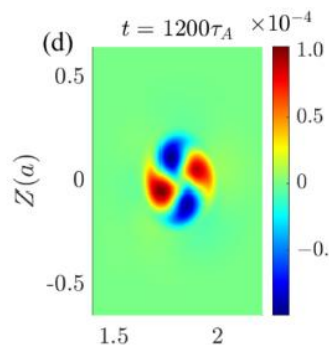
Precessional resonance is satisfied for $n=1, 2, 3$ modes

- $n\omega_\phi = \omega$ is satisfied for $m/n=1/1, 2/2, 3/3$ modes

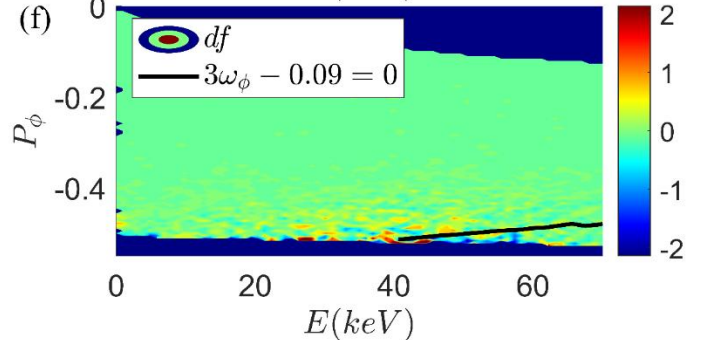
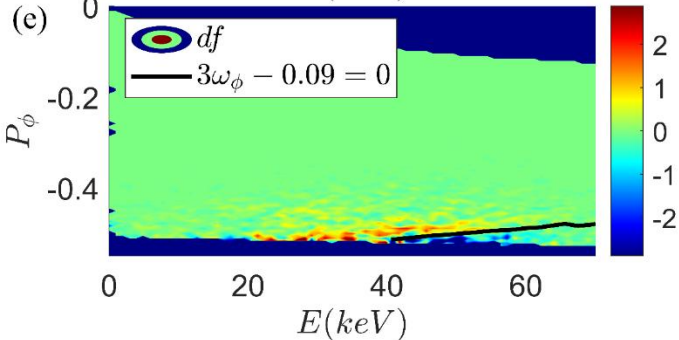
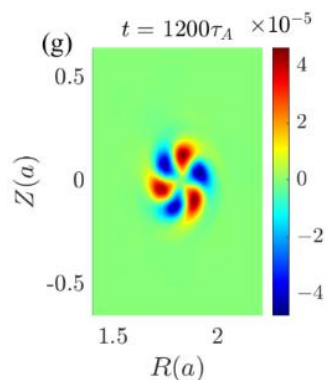
$m/n=1/1$



$m/n=2/2$

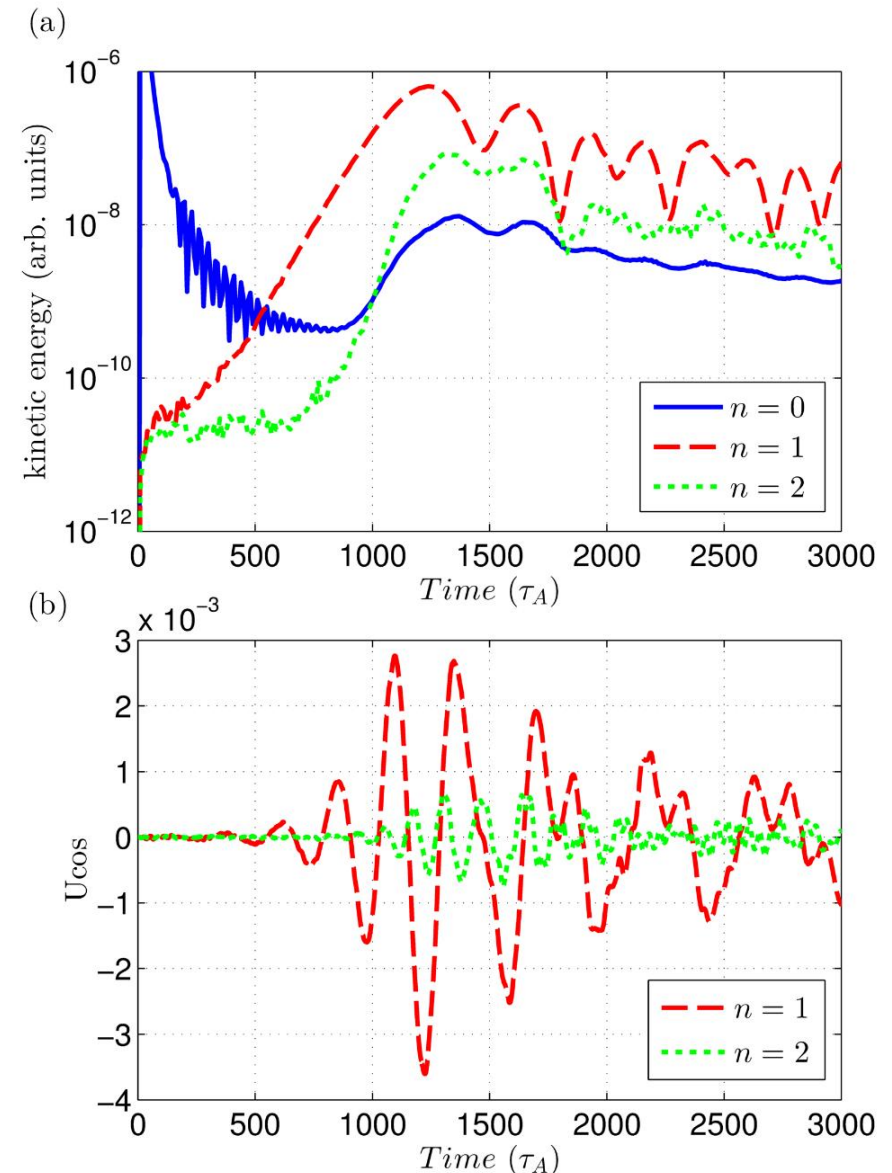


$m/n=3/3$



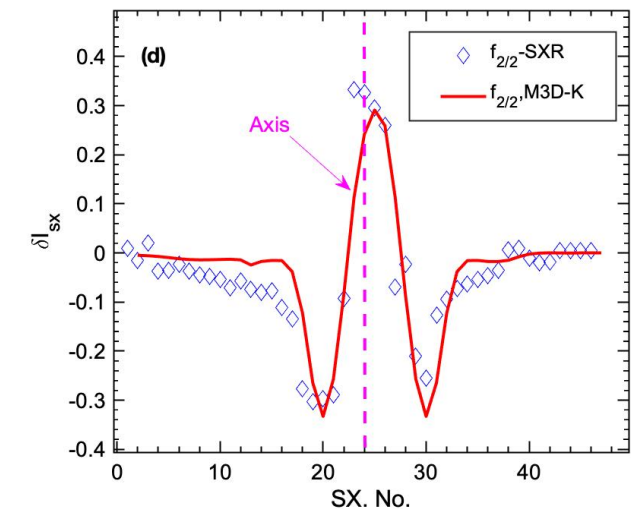
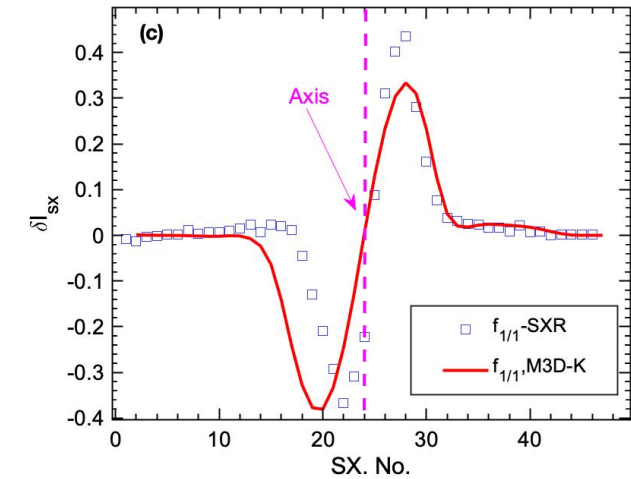
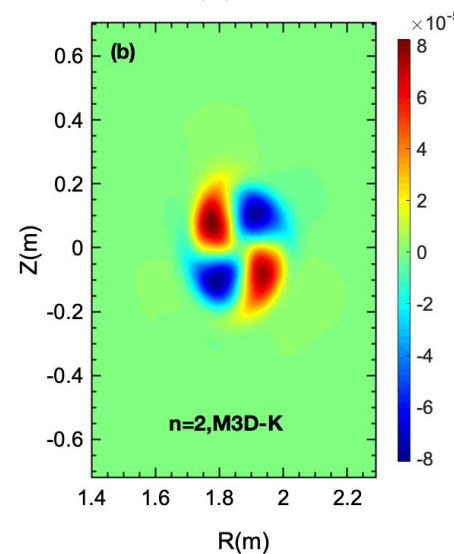
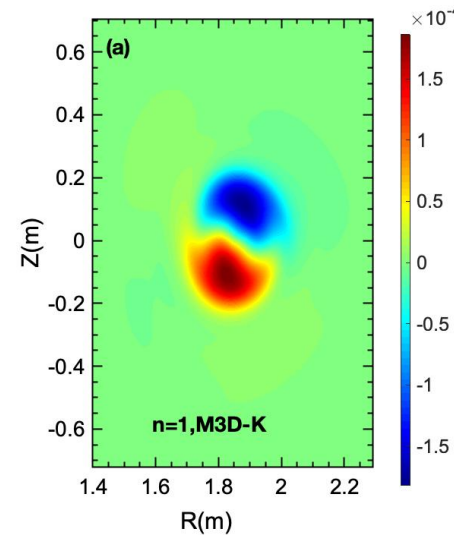
Kinetic energy evolution

- **Linear: $n=1$ mode is unstable, $n=2, 3$ modes are stable.**
- **Nonlinear evolution keeping from $n=0$ to $n=2$ shows that $n=2$ fishbone grows coupled to $n=1$ fishbone**
- **The $m/n=2/2$ fishbone is force-driven by the $m/n=1/1$ fishbone.**

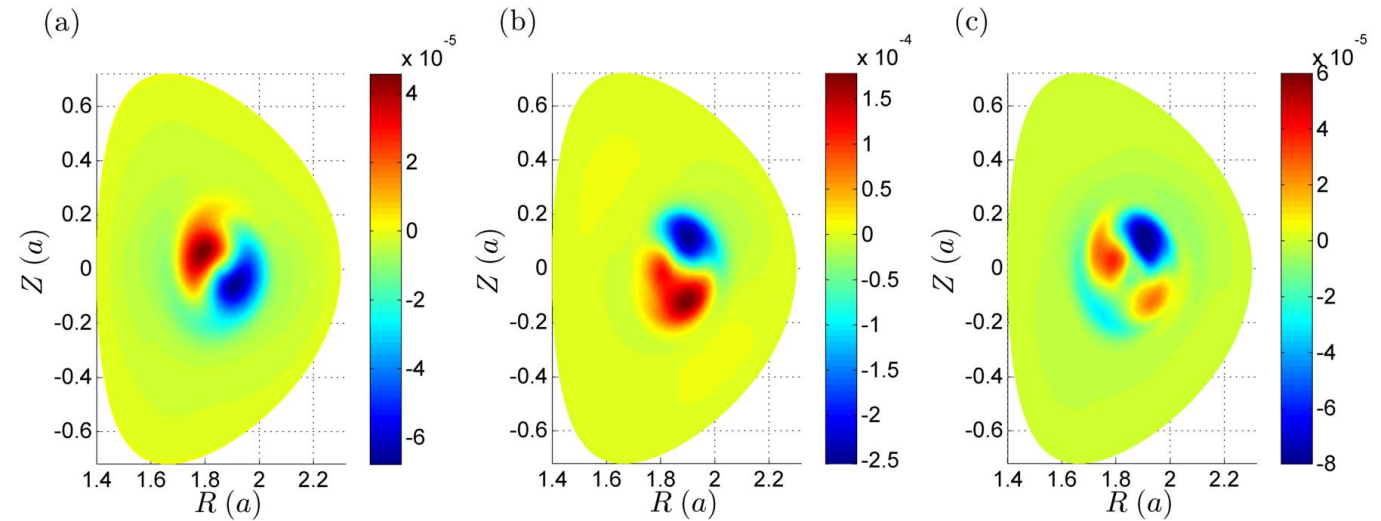
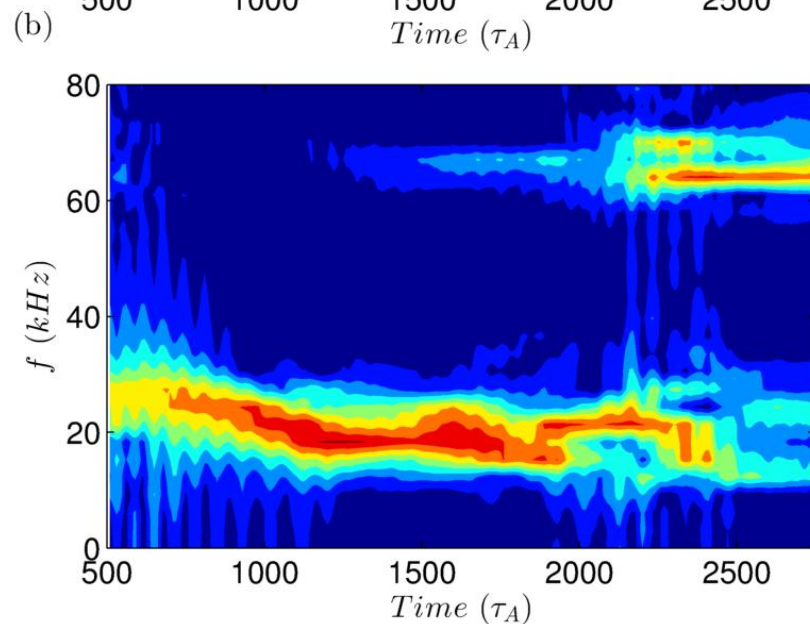
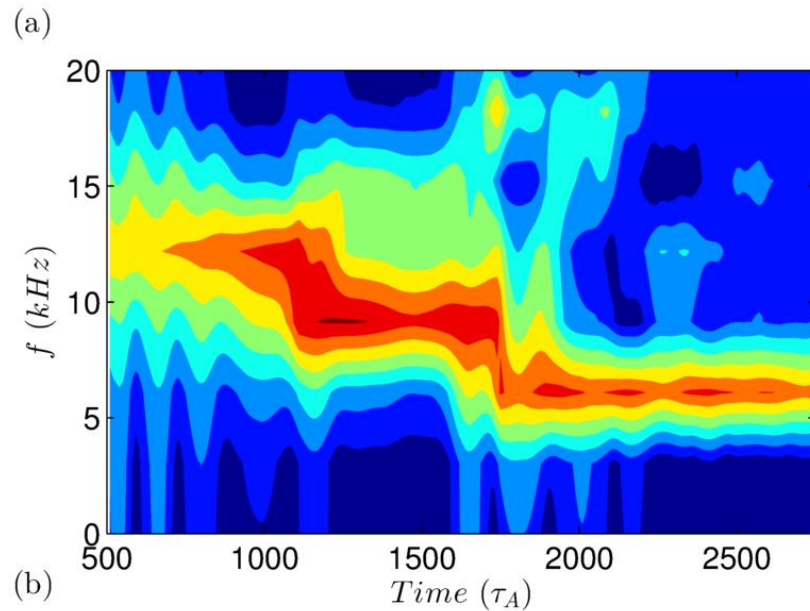


Mode structure in comparison with experiment

- The pressure perturbation structure of the $m/n=1/1$ and $m/n=2/2$ fishbones simulated by M3D-K code are shown in figures (a) and (b)
- Figures (c) and (d) show good agreements between simulation and experiment.



Mode frequency and structure evolution



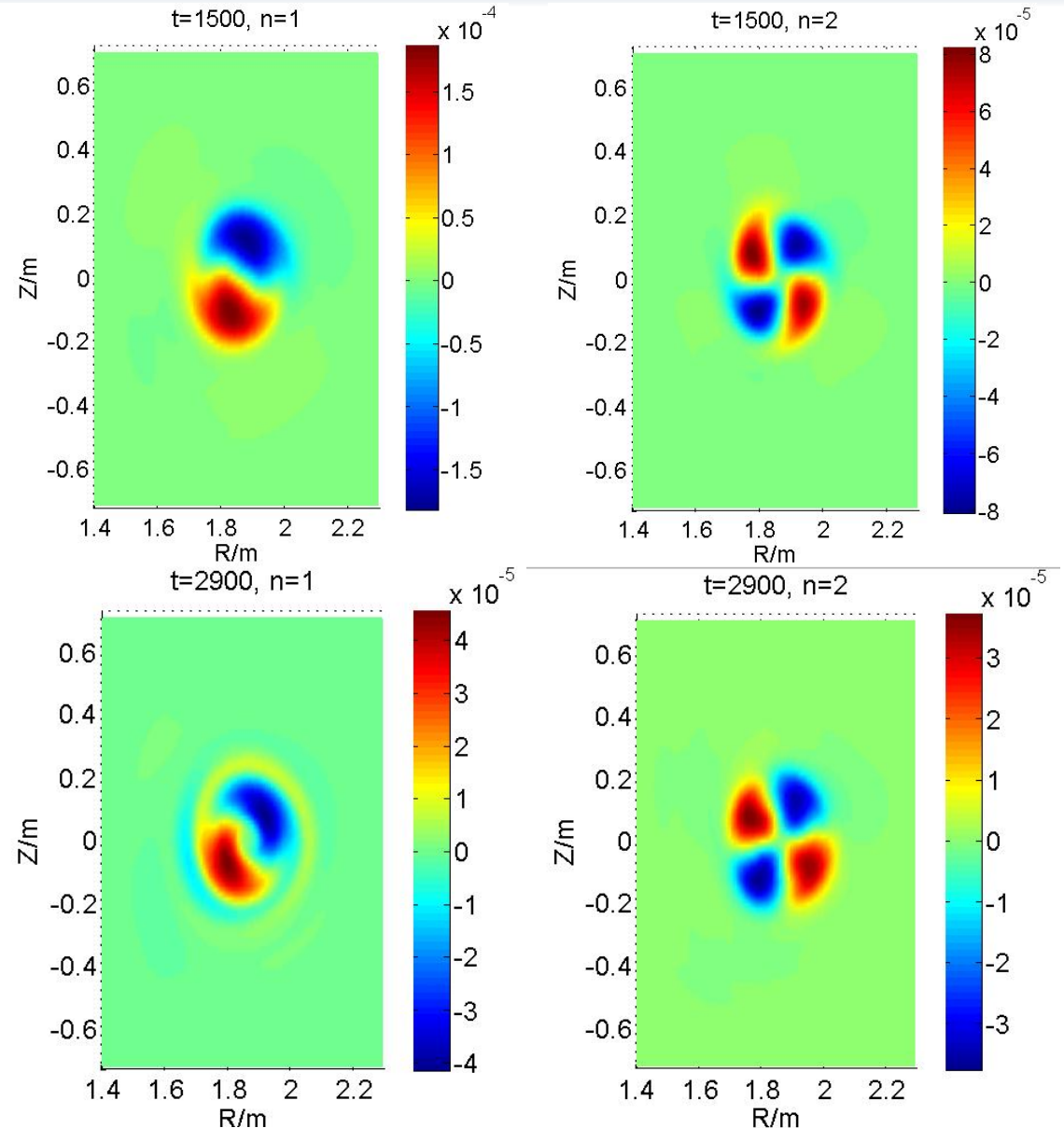
- The frequency of the $m/n=2/2$ fishbone is around twice of the $m/n=1/1$ fishbone, and they chirp down together.
- At later nonlinear phase, the frequency of the $m/n=2/2$ fishbone chirps up and it transits to a high frequency BAE.

n=1 and n=2 mode structures

- **n=1 mode: more twisted at t=2900**
- **n=2 mode: more twisted at t=1500**
- **High frequency n=2 mode at t=2900 is identified as BAE,**

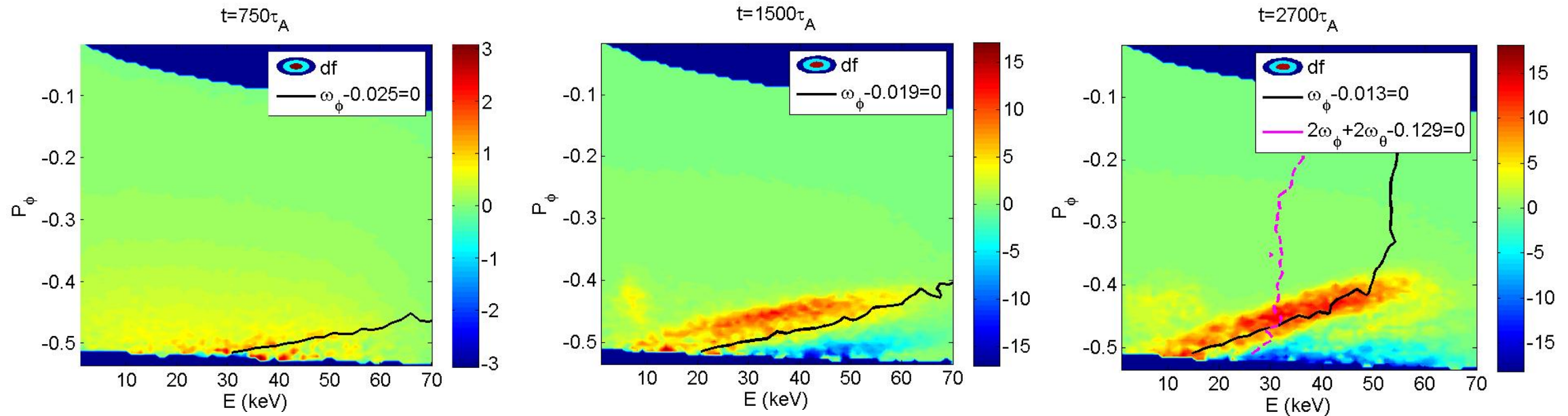
- **t = 2 9 0 0 : $\omega_{n=2} = 0.138\omega_A$, consistent with BAE accumulation point in MHD limit $\omega_{BAE} =$**

$$\sqrt{\gamma\beta}\omega_A = 0.140\omega_A$$



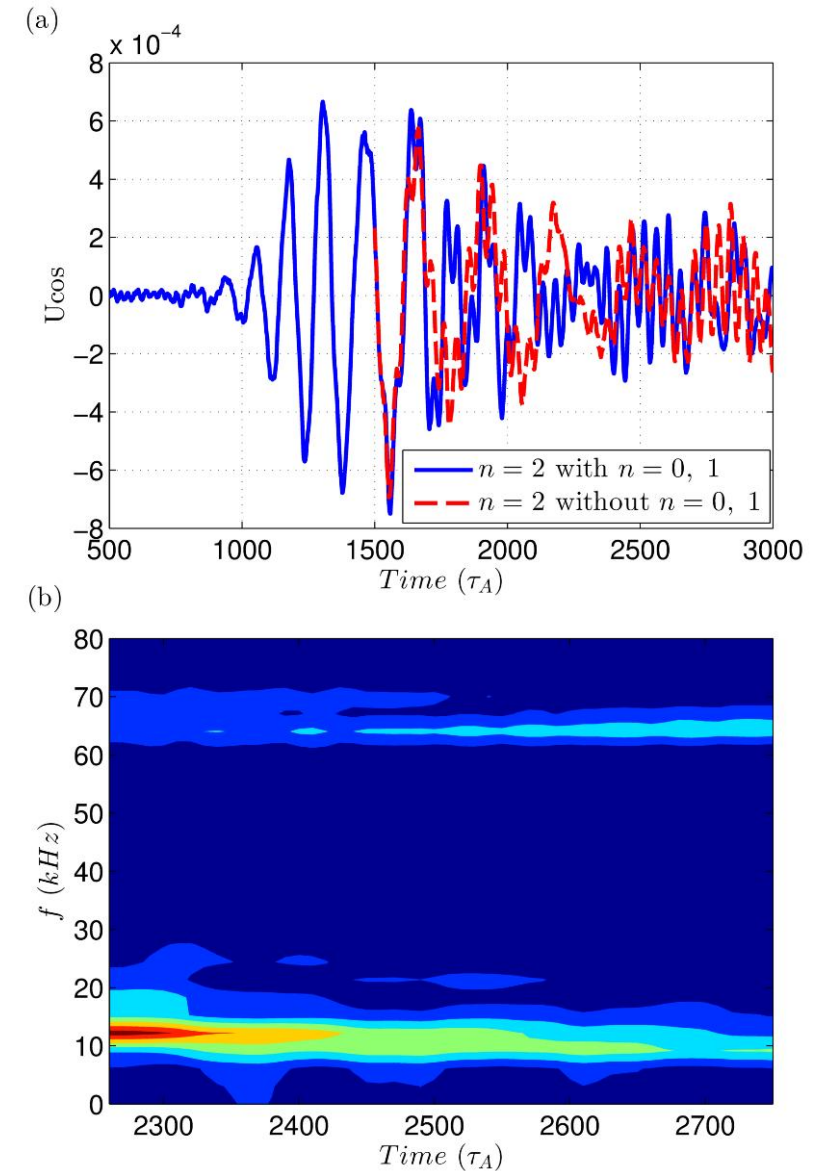
$m/n=2/2$ BAE is excited due to EP redistribution

- ✓ $t=750\tau_A$: linear resonant condition for both $m/n=2/2$, $1/1$ fishbones
- ✓ $t=1500\tau_A$: early nonlinear phase, the frequency of $m/n=2/2$ fishbone chirps down together with $m/n=1/1$ fishbone
- ✓ $t=2700\tau_A$: $m/n=2/2$ BAE is excited nonlinearly due to EP transport in phase space

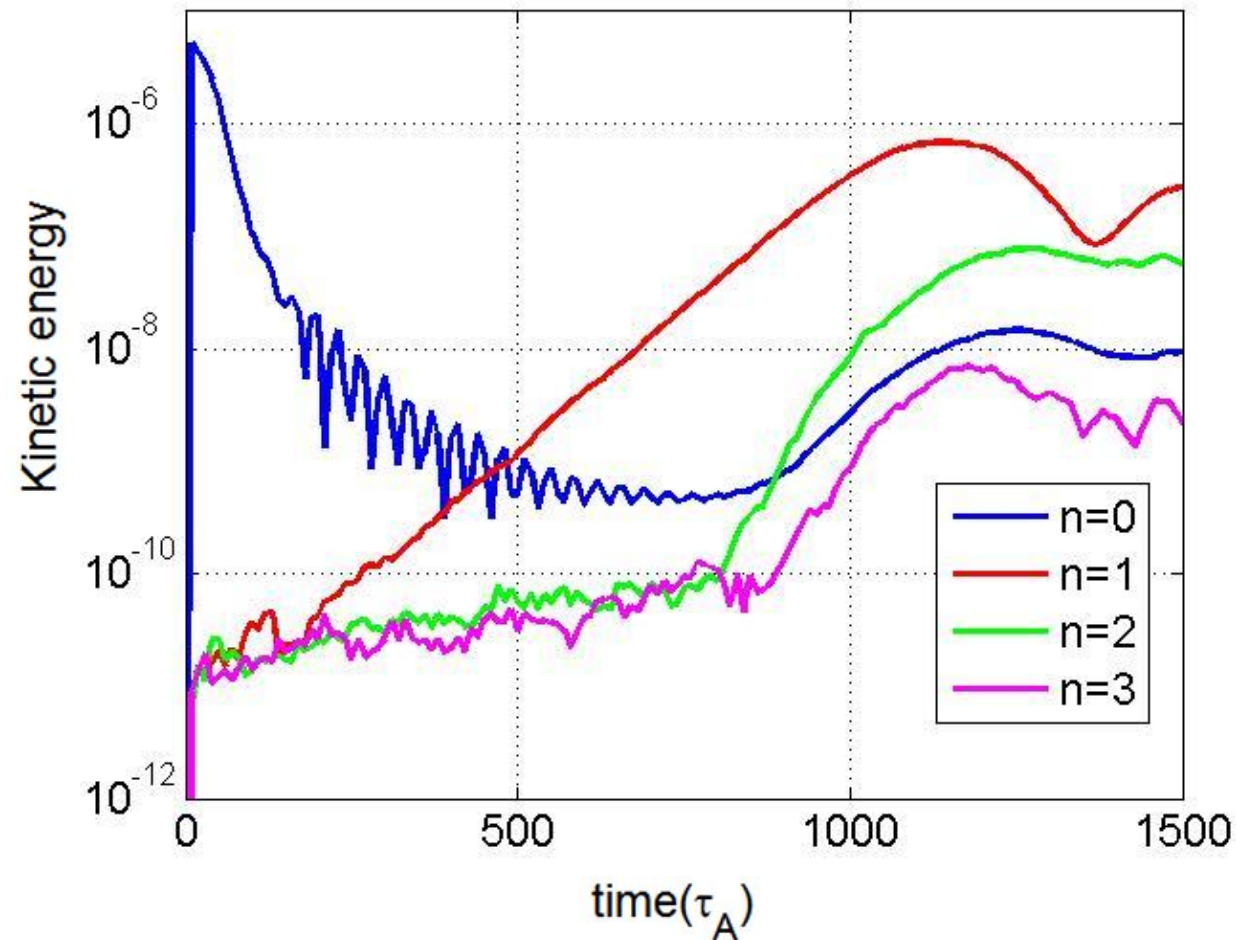


EP nonlinearity is dominant for fishbone saturation

- The comparison between the amplitude of $n=2$ component with and without MHD nonlinearity shows that EP nonlinearity is dominant for the $n=2$ fishbone saturation and transition to BAE.



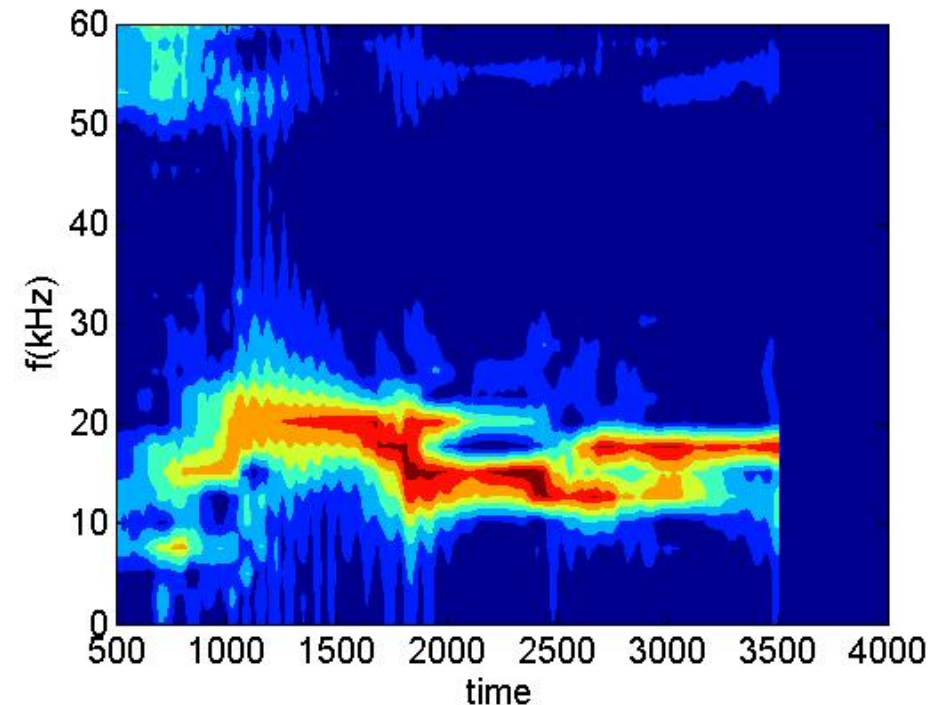
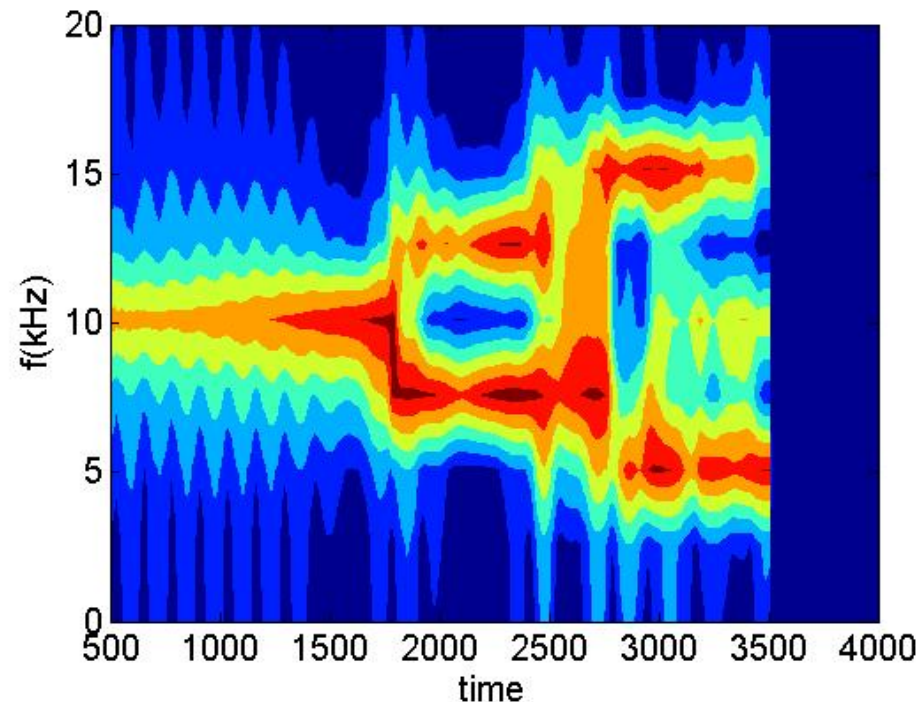
Simulation results keeping up to $n=3$ component



- **Kinetic energy of $n=3$ component is much smaller than $n=1$ and $n=2$ components, confirming that keeping up to $n=2$ mode in the simulation is enough, also consistent with experiment.**

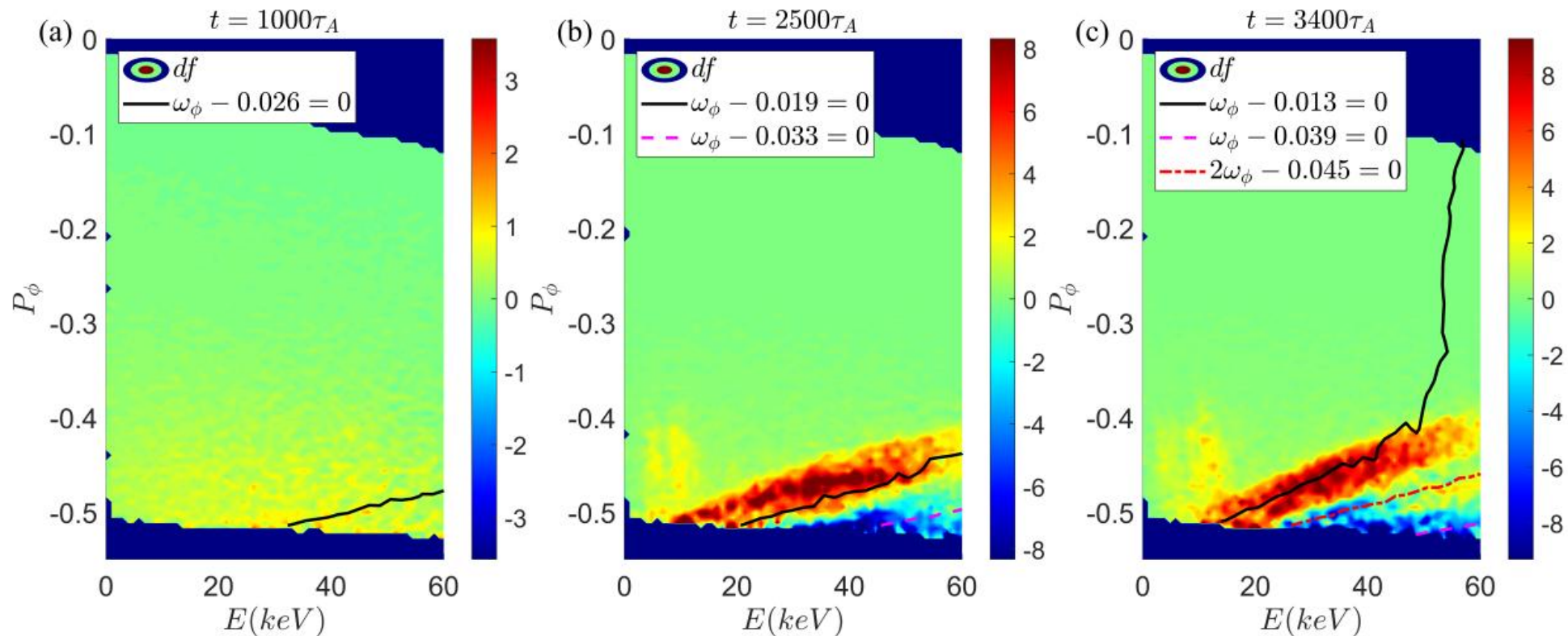
The frequency evolution changes with lower EP fraction

- **Baseline case: $P_{\text{hot},0}/P_{\text{total},0}=0.3$, lower EP fraction case: $P_{\text{hot},0}/P_{\text{total},0}=0.25$**
- **The frequency of n=1 fishbone chirps up and down**
- **The n=2 fishbone does not transit to BAE.**



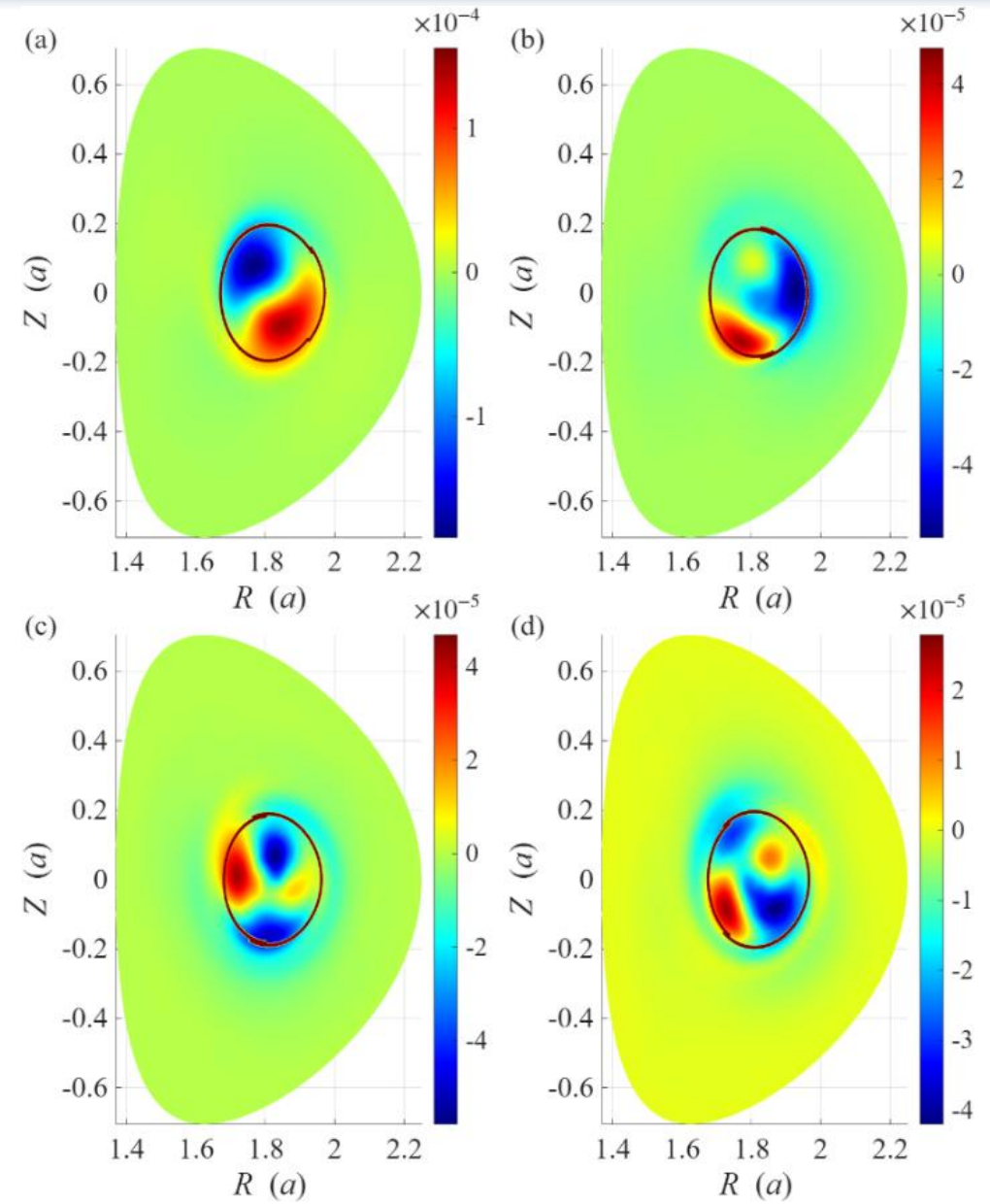
Resonance lines move with hole-clump structure

- The frequency of $n=1$ fishbone chirps up and down together with hole-clump structure formed in EP phase space
- Resonance lines move with EP hole-clump structure in phase space.



Nonlinear mode structure is affected by $m/n=2/2$ component

- **(a): Linear mode structure with $m=n=1$**
- **(b): early nonlinear phase: mode structure affected by $m=n=2$ component**
- **(c)-(d): fishbone with $m=n=2$ component becomes more obvious**



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Conclusion

The fishbones with $n=1$ and $n=2$ components on EAST have been simulated by M3D-K code.

- **$n=2$ mode is linearly stable, but nonlinearly grows coupled with $n=1$ mode.**
- **The $m/n = 2/2$ fishbone frequency is almost twice of the $m/n = 1/1$ fishbone, and both fishbone frequencies chirp down together.**
- **The $n=2$ fishbone transits to a high frequency BAE at later nonlinear phase.**
- **EP nonlinearity is dominant for $n=2$ mode saturation and transition to BAE.**

Thank you for your attention!

